

1/ 2013.10.10 (Chap 5 Context-free Grammars)

quadruple - (4요소)

Def. A CFG $G = (N, T, P, S)$ where

(1) $N \dots$ is a set of nonterminals (variables, syntactic categories)
 (Vintext) Symbols

(2) $T \dots$ is a " terminal symbols.
 (input)

$N \cap T = \emptyset$. $V = N \cup T \dots$ general symbols

(3) $P \dots$ a set of production rules (문법규칙)

$(A, \alpha) \in P \implies A \rightarrow \alpha \in P \quad (A, \alpha) \in N \times V^* = N \cup (N \cup T)^*$
 $A \in N, \alpha \in V^* = (N \cup T)^*$

(4) $S \in N$, a distinguish nonterminal call start symbol.
 axiom

Context-Free $G = (N, T, P, S)$

문법 자유 $(B \in N, \beta \in (N \cup T)^*)$
 \Rightarrow derive: $\alpha, \gamma \in V^*, B \rightarrow \beta \in P$

derivation

$\alpha B \gamma \Rightarrow \alpha \beta \gamma \quad (B \rightarrow \beta \in P)$

We define \Rightarrow^n ($n \geq 0$)

$\alpha \Rightarrow_B^0 \alpha$ (basis) $\alpha \in V^*$

If $\alpha \Rightarrow^{n-1} \beta, \beta \Rightarrow^1 \gamma$. Then $\alpha \Rightarrow^n \gamma$ ($n \geq 0$) (recursion)

We define \Rightarrow^* and \Rightarrow^+

$\Rightarrow^* \stackrel{\text{def}}{=} \bigcup_{i \in \mathbb{N}_0} \Rightarrow^i$

where $\mathbb{N}_0 = \{0, 1, 2, \dots\}$ (ref. & trans) class

$\Rightarrow^+ \stackrel{\text{def}}{=} \bigcup_{i \in \mathbb{N}_1} \Rightarrow^i$

" $\mathbb{N}_1 = \{1, 2, 3, \dots\}$ (trans) class

0번 이상 closure / 1번 이상 positive closure

3
 Def. $G = (N, T, P, S)$ $L(G) = \{x \in T^* \mid S \Rightarrow^* x\}$
 languages of G defined by G generated by G
 parse tree \downarrow
 class of languages $\left\{ \begin{array}{l} \text{content-free} \\ \text{regular} \end{array} \right.$
 Automata $\left\{ \begin{array}{l} \text{F.A.} \end{array} \right.$ Grammars $\left\{ \begin{array}{l} \text{CFG} \end{array} \right.$

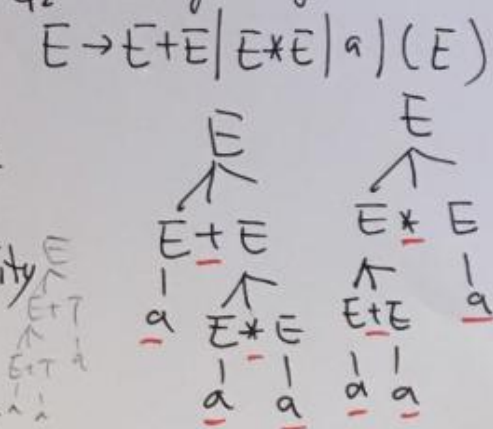
sentential form, sentence
 $S \Rightarrow \alpha \in V^*$ $S \Rightarrow x \in T^*$

Notational Convention $\frac{L}{\neq}$

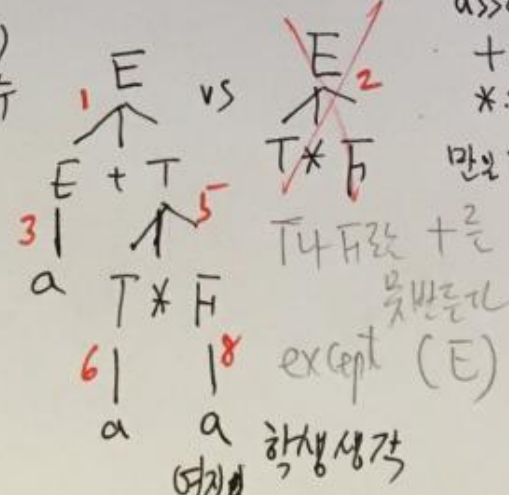
$a, b, c, \dots \in T$
 $x, y, z, uv, w, \dots \in T^*$
 $A, B, C, \dots \in N$
 $X, Y, Z, \dots \in V = N \cup T$

if $\exists x \in L(G)$
 \exists Parse tree for x in G .
 Ambiguous grammar G_2

G_1 :
 $E \rightarrow E + T \mid T * F \mid a \mid (E)$
 $T \rightarrow T * F \mid a \mid (E)$ precedence
 $F \rightarrow a \mid (E)$
 $+ < *$
 associativity
 $+$: left
 $*$: \downarrow
 만 $T \rightarrow F * T$

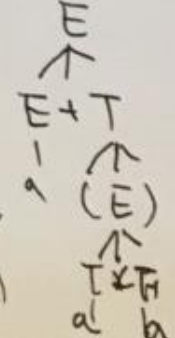


$a + a * a \in L(G_2)$



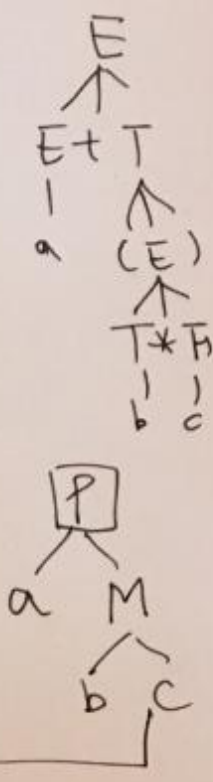
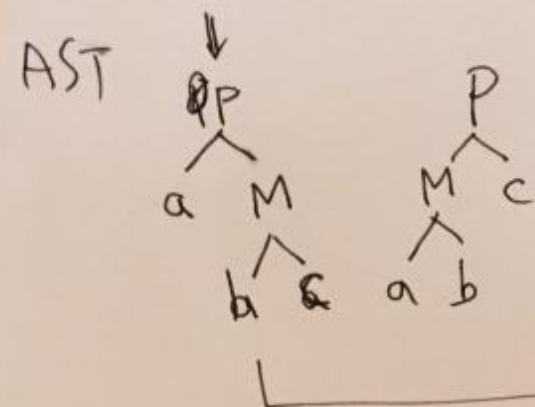
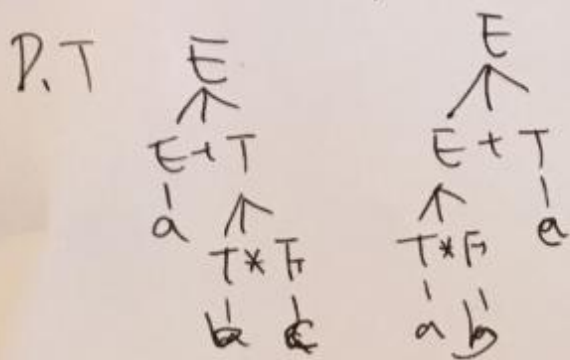
$E \Rightarrow E + E \Rightarrow a + E \Rightarrow a + E * E \Rightarrow a + a * E \Rightarrow a + a * a \in T^*$

$a + (a * a) \Rightarrow$
 $(a + a) * a \Rightarrow$
 $(a + a * a) \times$



3) Abstract syntax Tree (AST) vs Parse Tree (G)

$$G = (N, T, P, S)$$



AST

~~(N, T, P, S)~~

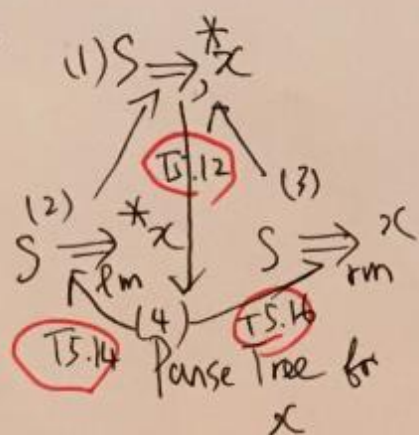
$P' \subseteq P$... subtree

$T' \subseteq T$... leaf

$$P' = \{ E \rightarrow E + T \mid T * F, T \rightarrow T + F \}$$

$$T' = \{ a \} + \{ *, (,) \}$$

5.2



$$(1) \equiv (2) \equiv (3) \equiv (4)$$

P.T. for x

$$S \xRightarrow{\pi_L} \alpha \in T^*$$

$$S \xRightarrow{\pi_R} \alpha \in T^*$$

$\pi_L \in P^*$... left parse of $\alpha \in T^*$

$\pi_R \in P^*$... **Reversal** of right parse of $\alpha \in T^*$

Ding & Ko's Book
Examples of CFG's.

→ 중간과제 - 위치 10/25(화)
전사합동 (E3-1) 오후 1:00 ~
총 공동강의실 (1501)