

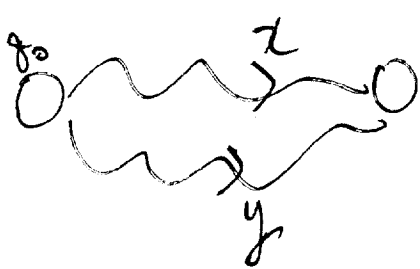
7/7 - 10/16) Minimum DFA & Context-Free Grammar (1)
 Chap 5

Skip Sec. 4.2 & ~~is in the~~ text.

Let $M = (Q, \Sigma, \delta, q_0, F)$ be a DFA.

We define $R_M \subseteq \Sigma^* \times \Sigma^*$

$(x, y) \in R_M$ if $\delta(q_0, x) = \delta(q_0, y) \in Q$ ~~is~~ right invariant equiv. rel.



R_M is equivalent partition on $\Sigma^* = |Q|$ index of R

Let A partition
 $\text{Part}(A) = \{\{a\} \mid a \in A\}, \rightarrow |A|$
 $= \{A\}$

ex) $A = \{a, b, c\}$
 $\{\{a\}, \{b\}, \{c\}\} = 3$
 $\{\{a, b, c\}\} = 1$

Let $L \subseteq \Sigma^*$ be a language over Σ .

$(L \in 2^{\Sigma^*})$
 We define $R_L \subseteq \Sigma^* \times \Sigma^*$

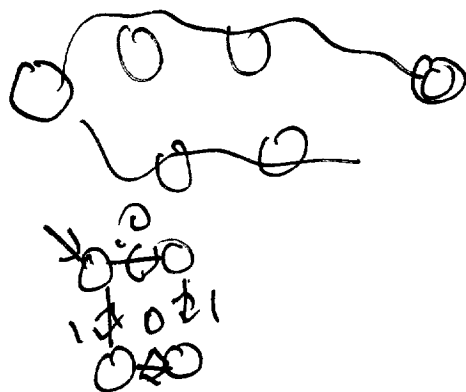
$(x, y) \in R_L$ if $(xz \in L \wedge yz \in L) \vee (xz \notin L \wedge yz \notin L)$

$$xz \in L \iff yz \in L$$

right inv. equi.

$R_M \quad R_L$

Myhill-Nerode Theorem



Chap. 5 Context-free Grammar (Language)

$$G = (N, \Sigma, P, S)$$

1) N - nonterminal symbols.
Set of

2) Σ - set of terminal (input) symbols

3) $P \subseteq N \times (N \cup \Sigma)^*$

$(A, \alpha) \in P, A \in N, \alpha \in (N \cup \Sigma)^*$

$A \rightarrow \alpha \in P$

Context-free grammar.

4) $S \in N : \overset{A}{\downarrow} \overset{B}{\downarrow} \overset{C}{\downarrow} \overset{D}{\downarrow} \overset{E}{\downarrow} \overset{F}{\downarrow} \overset{G}{\downarrow} \overset{H}{\downarrow} \overset{I}{\downarrow} \overset{J}{\downarrow} \overset{K}{\downarrow} \overset{L}{\downarrow} \overset{M}{\downarrow} \overset{N}{\downarrow} \overset{O}{\downarrow} \overset{P}{\downarrow} \overset{Q}{\downarrow} \overset{R}{\downarrow} \overset{S}{\downarrow} \overset{T}{\downarrow} \overset{U}{\downarrow} \overset{V}{\downarrow} \overset{W}{\downarrow} \overset{X}{\downarrow} \overset{Y}{\downarrow} \overset{Z}{\downarrow}$

$$L(G) = \{x \in \Sigma^* \mid S \Rightarrow^* x\}$$

$\Rightarrow^0 : \alpha \Rightarrow^0 \alpha, \alpha \in (N \cup \Sigma)^*$ Basis

$\Rightarrow^{n+1} : \Rightarrow^n, A \rightarrow \alpha \in P$ recursion

$$P \subseteq N \times \Sigma^*(N \cup \Sigma)^*$$

$A \in N$
 $x \in \Sigma^*$

(A, xB)

$A \rightarrow xB$

right linear gram.

left linear "

$A \rightarrow Bx$

$\epsilon \in P \rightarrow \epsilon \mid 0 \mid 1$

$0 \mid 0 \mid 1 \mid P_1$