

2007 Spring CS204 Homework #4

1. Exercise 3.1.14 (b)

1	3	4	5	6	8	9	11
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There is no 7 in the list.

2. Exercise 3.1.42

Write the selection sort algorithm in pseudocode using the syntax of the text or the syntax you learned in the class.

procedure selection sort(a_1, a_2, \dots, a_n ; distinct integers with $n \geq 2$)

$i := 1$;

do ($i < n$)

$\text{min} := i$;

$j := i + 1$;

 do ($j \leq n$)

 if ($a_j < a_{\text{min}}$) $\text{min} := j$; fi;

$j := j + 1$

 od;

$a_i, a_{\text{min}} := a_{\text{min}}, a_i$;

$i := i + 1$;

od;

3. Exercise 3.2.4

$$\forall x > 1, |2^{x+17}| \leq 7|3^x|$$

that is, $C = 7, k = 1$.

2^{x+17} is $O(3^x)$ with the witness $C = 7, k = 1$.

4. Exercise 3.2.10

i) x^3 is $O(x^4)$

$$\forall x > 1, x^3 \leq x^4 \text{ (witness } C = 1, k = 1)$$

ii) x^4 is not $O(x^3)$

모든 x 에 대해 $|x^4| \leq C|x^3|$ 를 만족시키는 C 가 존재하지 않는다.

임의의 C 에 대해 $|x^4| \leq C|x^3|$ 를 만족시키지 않는 x 가 존재한다. ($x = C + 1$)

There does not exist C such that $|x^4| \leq C|x^3|$ for every x .

For arbitrary C , there exists x that does not satisfy $|x^4| \leq C|x^3|$.

5. Exercise 3.2.20

a) $O(n^3 \log n)$

b) $O(6^n)$

c) $O(n^n n!)$